

Fermion Condensate Model of Electroweak Interactions

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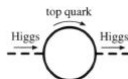
- 1 Introduction, motivation
- 2 Fermion Condensate Model
 - Gap equations, masses, mixing
 - Phenomenology
- 3 Conclusion, Outlook

BSM - Solutions to the Hierarchy Problem

Standard Model is incomplete

- theory problems & phenomenology indications

$$\delta M_H^2 \sim -\frac{3G_F}{2\sqrt{2}\pi^2} m_{top}^2 \Lambda^2 \sim -(0.2\Lambda)^2$$



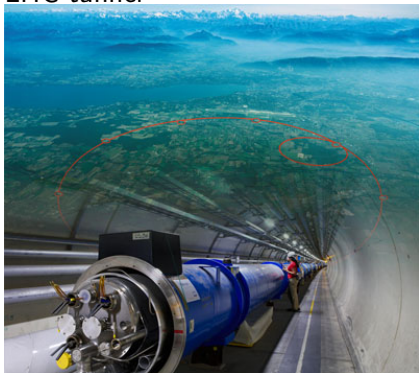
Solutions:

- **Supersymmetry**, perturbative cancellations
Fermion-boson symmetry (softly broken) $\Lambda \sim m_{\cancel{g}_{usy}} \simeq m_{susy} - m$
- **Dynamical symmetry breaking**
technicolor-like models, composite Higgs
- **Extra dimensions**
Apparent Planck scale large, geometrical solution
- **Little-Higgs**
Higgs: (Pseudo GB), B-B and F-F cancellation

LHC - most important tasks

- 1 Reveal the mechanism of EWSB
Find the Higgs, if it exists!
- 2 Search for new physics at the TeV scale
- 3 Dark matter candidates
- 4 Anything unexpected

LHC tunnel



The new physics is unknown, model dependent constraints

⇒ Important to check alternative scenarios.

Dynamical Symmetry Breaking w/ Vector-like Fermions

- Low energy non-renormalizable, effective model
Without elementary scalar
- New fermions are non-chiral, differs from technicolor
- Dynamical condensate breaks EW symmetry.
Mixing between doublet & singlet rep's is essential.
- Higgs: composite state.

G. C., E. Lendvai and G. Pócsik, EPJ C46 (2006)

G. C., E. Lendvai, J.Phys. G34 (2007), EPJ C58 (2008).

G. Cynolter and E. Lendvai, arXiv:1002.4490 [hep-ph]

SM elementary Higgs (sector) replaced by new vector-like fermions

$$\begin{pmatrix} \Phi^{(+)} \\ \Phi^{(0)} \end{pmatrix} \rightarrow \left\{ \begin{array}{l} \Psi_S, \quad T = Y = 0, \text{ singlet} \\ \Psi_D = \begin{pmatrix} \Psi_D^+ \\ \Psi_D^0 \end{pmatrix}, \quad T = \frac{1}{2}, Y = 1, SU_L(2) \text{ doublet} \end{array} \right.$$

Non-chiral representations \Rightarrow anomaly free

Similar extra fermions investigated

MSSM neutralino sector,

 [R. Barbieri, L.J. Hall, V.S. Rychkov: Improved naturalness..PRD74 \(2006\)](#)

 [P.J. Fox, L.J. Hall, M. Papucci,..., Dark matter... JHEP 0711](#)

 [M. Cirelli, A. Strumia,...Minimal dark matter, Nucl. Phys. B **753** \(2006\)](#)

 [Rakhi Mahbubani, Leonardo Senatore, Phys. Rev. **D73**: 043510 \(2006\).](#)

 [F. D'Eramo, Dark Matter + Higgs phys., Phys.Rev.D76:083522 \(2007\).](#)

 and many other ...

Lagrangian (new terms)

$$L_{\Psi} = i\bar{\Psi}_D D_{\mu} \gamma^{\mu} \Psi_D + i\bar{\Psi}_S \partial_{\mu} \gamma^{\mu} \Psi_S - m_{0D} \bar{\Psi}_D \Psi_D - m_{0S} \bar{\Psi}_S \Psi_S + \lambda_1 (\bar{\Psi}_D \Psi_D)^2 + \lambda_2 (\bar{\Psi}_S \Psi_S)^2 + 2\lambda_3 (\bar{\Psi}_D \Psi_D) (\bar{\Psi}_S \Psi_S),$$

$SU_L(2) \times U_Y(1)$ covariant derivative $D_{\mu} = \partial_{\mu} - i\frac{g}{2} \tau A_{\mu} - i\frac{g'}{2} B_{\mu}$,
 A_{μ}, B_{μ} and g, g' gauge fields and couplings

- Dimensionful couplings $\lambda_3 = \tilde{\lambda}_3/\Lambda^2$, m_{0D}, m_{0S} allowed.
- Non-renormalizable effective theory with a Λ (physical) cutoff.
- Further 4-fermion couplings are possible, argument unchanged.
- Do not mix w/ standard fermions, conserved new fermion-number (parity).

Condensates formed, if $\lambda_i > \lambda_i^{crit}$:

$$\langle \bar{\Psi}_{D\alpha}^0 \Psi_{D\beta}^0 \rangle_0 = a_1 \delta_{\alpha\beta},$$

$$\langle \bar{\Psi}_{D\alpha}^+ \Psi_{D\beta}^+ \rangle_0 = a_+ \delta_{\alpha\beta}, \quad \langle \bar{\Psi}_S \Psi_D \rangle_0 = \left\langle \begin{pmatrix} \bar{\Psi}_S \Psi_D^+ \\ \bar{\Psi}_S \Psi_D^0 \end{pmatrix} \right\rangle_0 = \begin{pmatrix} 0 \\ a_3 \end{pmatrix} \neq 0$$

$$\langle \bar{\Psi}_{S\alpha} \Psi_{S\beta} \rangle_0 = a_2 \delta_{\alpha\beta},$$

Self-consistent masses and mixing generated if $\lambda_i > \lambda_i^{crit}$.

„Diagonal” mass

$$\Psi_D^0 \quad \times \quad m_1 \quad \Psi_D^0 = \frac{\Psi_D^0 \text{ loop } \Psi_D^0}{\lambda_1} + \frac{\Psi_D^+ \text{ loop } \Psi_D^+}{\lambda_1} + \frac{\Psi_S \text{ loop } \Psi_S}{\lambda_3}$$

Non-diagonal condensate triggers mixing and EWSB

$$\Psi_D^0 \quad \times \quad m_3 \quad \Psi_S = \frac{\Psi_D^0 \text{ loop } \Psi_S}{\lambda_3}$$

Gap equations II

Condensates generate dynamical masses and mixing in L

$$L_\Psi \rightarrow L_\Psi^{\text{lin}} = -m_+ \overline{\Psi}_D^+ \Psi_D^+ - m_1 \overline{\Psi}_D^0 \Psi_D^0 - m_2 \overline{\Psi}_S \Psi_S - m_3 \left(\overline{\Psi}_D^0 \Psi_S + \overline{\Psi}_S \Psi_D^0 \right)$$

$$m_+ = m_{0D} - 6\lambda_1 a_+ - 8(\lambda_1 a_1 + \lambda_3 a_2) = m_1 + 2\lambda_1 (a_+ - a_1) \quad (1)$$

$$m_1 = m_{0D} - 6\lambda_1 a_1 - 8(\lambda_1 a_+ + \lambda_3 a_2), \quad (2)$$

$$m_2 = m_{0S} - 6\lambda_2 a_2 - 8\lambda_3 (a_1 + a_+), \quad (3)$$

$$m_3 = 2\lambda_3 a_3. \quad (4)$$

$m_3 \neq 0$ neutral comp. of the doublet and singlet fermion mix.

\Rightarrow Electroweak symmetry breaking.

$$\overline{\Psi}_D^0 \text{---} m_1 \text{---} \Psi_D^0 = \overline{\Psi}_D^0 \text{---} \lambda_1 \text{---} \Psi_D^0 + \overline{\Psi}_D^0 \text{---} \lambda_1 \text{---} \Psi_D^+ + \overline{\Psi}_D^0 \text{---} \lambda_3 \text{---} \Psi_S$$

$$\overline{\Psi}_D^0 \text{---} m_3 \text{---} \Psi_S = \overline{\Psi}_D^0 \text{---} \lambda_3 \text{---} \Psi_S$$

Physical fields Ψ_1, Ψ_2 és $\Psi_+ = \Psi_D^+$

Diagonalized fields and (physical masses)

$$\Psi_1 = c \Psi_D^0 + s \Psi_S, \quad (M_1)$$

$$\Psi_2 = -s \Psi_D^0 + c \Psi_S, \quad (M_2)$$

$s = \sin \Phi$, $c = \cos \Phi$, mixing angle Φ .

Condensates of physical fields

$$\frac{\delta_{\alpha\beta}}{4} l_i = \langle \bar{\Psi}_{i\alpha} \Psi_{i\beta} \rangle_0 = -\frac{\delta_{\alpha\beta}}{8\pi^2} M_i \left(\Lambda^2 - M_i^2 \ln \left(1 + \frac{\Lambda^2}{M_i^2} \right) \right) \quad i=1,2,+.$$

$$c \cdot s (M_1 - M_2) = 2\lambda_3 c \cdot s (l_1 - l_2),$$

$$c^2 M_1 + s^2 M_2 = -\lambda_1 (6(c^2 l_1 + s^2 l_2) + 8l_+) - 8\lambda_3 (s^2 l_1 + c^2 l_2),$$

$$s^2 M_1 + c^2 M_2 = -6\lambda_2 (s^2 l_1 + c^2 l_2) - 8\lambda_3 (c^2 l_1 + s^2 l_2 + l_+),$$

$$M_+ = -\lambda_1 (8(c^2 l_1 + s^2 l_2) + 6l_+) - 8\lambda_3 (s^2 l_1 + c^2 l_2).$$

Symm. breaking solution ($\sin 2\Phi \neq 0$), if $|\lambda_3| > \lambda_3^{crit} = \frac{\pi^2}{\Lambda^2}$.

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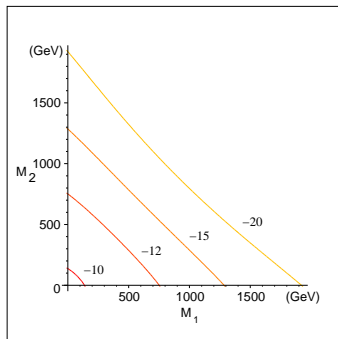
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Symmetry breaking solutions



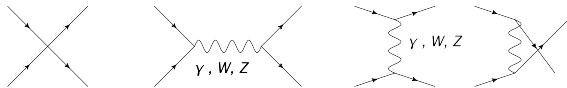
λ_3 contours on M_1 - M_2 plane $\lambda_3^{crit} = -\pi^2/\Lambda^2$
 $\lambda_3 = \{-10, -12, -15, -20\} \cdot 1/\Lambda^2$, $\Lambda = 3$ TeV.

Mixing is essential $2c \cdot s = \sin 2\phi \neq 0$.

$$0 = (M_1 - M_2) c \cdot s \left(\frac{1}{\lambda_3} + \frac{\Lambda^2}{\pi^2} - \frac{M_1^3 \ln \left(1 + \frac{\Lambda^2}{M_1^2} \right) - M_2^3 \ln \left(1 + \frac{\Lambda^2}{M_2^2} \right)}{M_1 - M_2} \right)$$

Perturbative unitarity

Consider $2 \rightarrow 2$ elastic scattering of $\Psi_{1,2}, \Psi^+$ new fermions
and $|\Re a_0| \leq \frac{1}{2}$ for $J=0$ partial wave

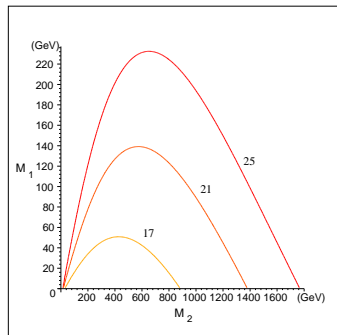


Dominant contribution from contact graph (+ γ, W, Z exchange)

$$\lambda_i s \leq 8\pi, \quad s \leq \Lambda^2$$

Most stringent for λ_2 coupling $\sim \lambda_2 (\bar{\Psi}_S \Psi_S)^2$.

Unitarity + Gap equations



λ_2 contours on M_1 - M_2 plane
 $\lambda_2 \leq 8\pi/\Lambda^2$, $\Lambda = 3 \text{ TeV}$, $m_{0D,0S} = 0$.

•

3 new fermions

Ψ_1, Ψ_2, Ψ_+

$M_1 \leq M_+ \leq M_2$

par's M_1, M_2, c^2 .

===== 2

===== +

===== 1

- favours small mixing (c^2)
- conserved global quantum number
- composite Higgs $\sim \bar{\Psi}_D \Psi_S$.

Standard fermion masses

Higgs Yukawa interactions \Rightarrow 4-fermion terms , $\Phi_{SM} \sim \bar{\Psi}_D \Psi_S$

$$L_f = g_f \left(\bar{\Psi}_L^f \Psi_R^f \right) \left(\bar{\Psi}_S \Psi_D \right) + g_f \left(\bar{\Psi}_R^f \Psi_L^f \right) \left(\bar{\Psi}_D \Psi_S \right),$$

dimensionful coupling constants $g_i = \tilde{g}_i / M^2$

The mixed condensate generates masses for the leptons and quarks.

The electron mass

$$m_e = -4g_e a_3 = -4\tilde{g}_e \frac{a_3}{M^2}.$$

Generates further $e^+ e^- \bar{\Psi}_S \Psi_D^0$ type interactions. ($g_e \sim m_e$)

Electron, ν_e doublet (\sim down type quarks)

$$L^I = g_e \left(\bar{\nu}_{eR} \bar{\Psi}_S \Psi_D^+ + \bar{e}_{LeR} \bar{\Psi}_S \Psi_D^0 + \bar{e}_{Re} \bar{\Psi}_D^+ \Psi_S + e_L \bar{\Psi}_D^0 \Psi_S \right).$$

Higgs Yukawa interactions \Rightarrow 4-fermion terms , $\Phi_{SM} \sim \bar{\Psi}_D \Psi_S$

$$L_f = g_f \left(\bar{\Psi}_L^f \Psi_R^f \right) \left(\bar{\Psi}_S \Psi_D \right) + g_f \left(\bar{\Psi}_R^f \Psi_L^f \right) \left(\bar{\Psi}_D \Psi_S \right),$$

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$$L' = g_e \left(\bar{\nu}_e \bar{\Psi}_S \Psi_D^+ + \bar{e}_L e_R \bar{\Psi}_S \Psi_D^0 + \bar{e}_R \nu \bar{\Psi}_D^+ \Psi_S + e_L \bar{\Psi}_D^0 \Psi_S \right).$$

Implications for Phenomenology

From Ψ_D doublet covariant kinetic term **renormalizable** int's.

$$L' = \bar{\Psi}_D^+ \gamma^\mu \Psi_D^+ (eA_\mu - e \cot 2\theta_W Z_\mu) + \frac{g}{2 \cos \theta_W} \bar{\Psi}_D^0 \gamma^\mu \Psi_D^0 Z_\mu + \frac{g}{\sqrt{2}} \left(\bar{\Psi}_D^+ \gamma^\mu \Psi_D^0 W_\mu^+ + \bar{\Psi}_D^0 \gamma^\mu \Psi_D^+ W_\mu^- \right).$$

Mixing implies

$$L' = \bar{\Psi}_D^+ \gamma^\mu \Psi_D^+ (eA_\mu - e \cot 2\theta_W Z_\mu) + \frac{e}{\sin 2\theta_W} Z_\mu (c^2 \bar{\Psi}_1 \gamma^\mu \Psi_1 + s^2 \bar{\Psi}_2 \gamma^\mu \Psi_2 - sc (\bar{\Psi}_1 \gamma^\mu \Psi_2 + \bar{\Psi}_2 \gamma^\mu \Psi_1)) + \left[\frac{g}{\sqrt{2}} W_\mu^+ (c \bar{\Psi}_D^+ \gamma^\mu \Psi_1 - s \bar{\Psi}_D^+ \gamma^\mu \Psi_2) + h.c. \right].$$

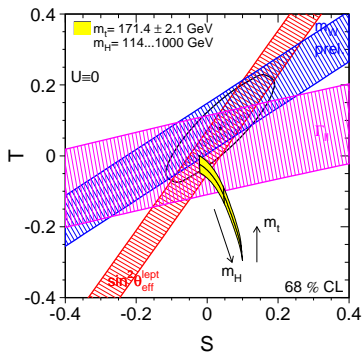
L_f^{mass} "Yukawa" int's are weaker than in SM

$$g_e \leq \sqrt{2h} \frac{m_e}{v} = \sqrt{2h} g_e^{SM} \quad h \text{ dimensionful!} \quad (L_H = h (D_\mu \Phi)^\dagger (D^\mu \Phi),)$$

Electroweak Precision Parameters

Oblique corrections, '92 Peskin-Takeuchi, ...

only via W^\pm, Z vacuum polarization if $M_{\text{New Physics}} \gg M_Z$



$$\frac{\alpha(M_Z)}{4s_W^2 c_W^2} S = \Pi'_{W_3 B}(0),$$

$$M_W^2 T = \Pi_{W_3 W_3}(0) - \Pi_{W^+ W^-}(0),$$

$$S = -0.10 \pm 0.10 \quad (-0.08)$$

$$T = -0.08 \pm 0.11 \quad (+0.09),$$

$$M_H^{\text{ref}} = 117(300) \text{ GeV}$$

S and T vanish for no mixing $c^2 = 0$

(non-degenerate vector-like doublet + singlet).

Expect small corrections for the solution of the gap equations.

S parameter in FCM

3 parameter, $M_1, M_2, c^2 = \cos^2 \Phi.$, T, S grows w/ c^2 .

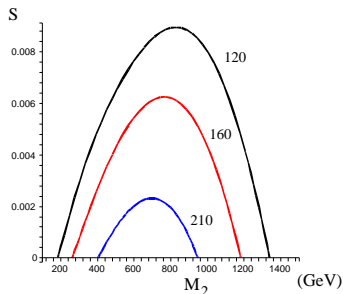


Figure: The max. value of the S parameter vs. M_2 for $M_1 = 120, 160, 210$ GeV. The 95 % C.L. bounds $[-0.296, 0.096]$ are outside the figure.

S parameter does not give constraints.

T parameter in FCM

3 parameter, $M_1, M_2, c^2 = \cos^2 \Phi$, ($M_+ \sim c^2 M_1 + s^2 M_2$),
 T, S grow with c^2 . $T > 0$ always

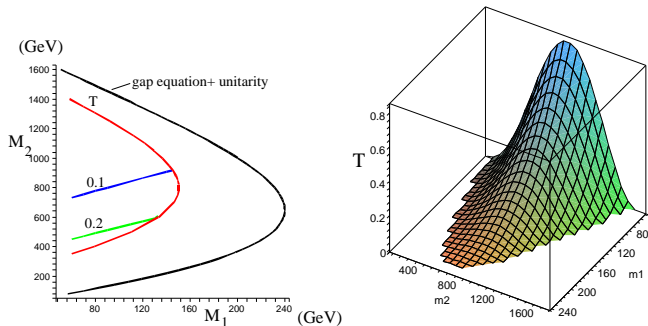
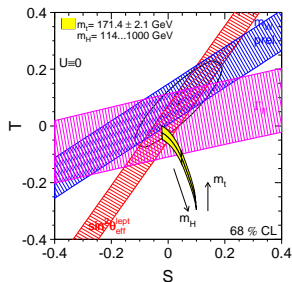


Figure: Constraints on (M_1, M_2) plane. Red curve: T gives the max. value of c^2 (@ 95 % C.L.) . Below the 0.1 (blue) and 0.2 (green) line c^2 can exceed 0.1 and 0.2. Right panel - the maximum value of T vs. (M_1, M_2) .

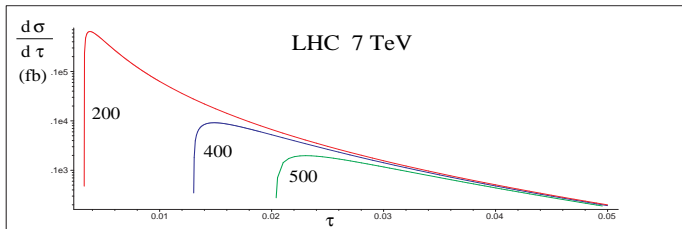
Heavy Higgs boson?

- Positive contrib'n to $T \rightarrow$ YES
- E.g. $M_H = 300$ GeV,
 $\Delta T = -0.09$
- Compensated by $\Delta T_{NP} = +0.1$
(160,800) GeV and $c^2 = 0.115$
 $M_+ \simeq 720$ GeV



Extension of the SM with vector type doublet fermions allows a heavy Higgs - "improved naturalness"

- PDG: doublet Ψ^+ $M_+ > 100$ GeV
neutral $M_{1,2} > 45$ GeV w/o assumptions
- LHC example: Drell-Yan production
 $q\bar{q} \rightarrow \gamma^*, Z^* \rightarrow \Psi^+\Psi^-$, tree level ($\hat{s} = \tau s$), without cuts



Total cross section	M_+ (GeV)	200	400	500
	σ (fb)	215	9.3	2.6

Small number of events with int. luminosity $10 - 100 \text{ pb}^{-1} - 1 \text{ fb}^{-1}$.

- **Dynamical SB Model** is proposed with extra **vector-like fermions** (doublet + singlet)
- **Mixed condensate**, mixing between diff. rep's. \Rightarrow EWSB
- **Composite Higgs, Allows a Heavy Higgs boson naturally**
- Unreachable at 7 TeV LHC with planned luminosity
- At 14 TeV LHC dedicated analysis needed (see Choi & Nojiri)
- Ψ_1 is an ideal dark matter candidate

Effective **doublet composite scalar** ($Y=1$) gives masses

$$\Phi = \begin{pmatrix} \Phi^+ \\ \Phi^0 \end{pmatrix} = \bar{\Psi}_S \Psi_D,$$

Φ kinetic term is generated in the low energy effective description (like in top-condensate models).

$$L_H = h (D_\mu \Phi)^\dagger (D^\mu \Phi) \quad \dim(h) = -4$$

$$h \Phi^{0\dagger} \Phi^0 \rightarrow h \langle \Phi^{0\dagger} \Phi^0 \rangle_0 = h (16a_3^2 - 4a_1 a_2) = \frac{v^2}{2},$$

get standard masses with, $v = (\sqrt{2} G_F)^{-1/2} = 254 \text{ GeV}$

$$m_W = \frac{gv}{2}, \quad m_Z = \frac{gv}{2 \cos \theta_W}.$$

- At 14 TeV LHC dedicated analysis
 - jetmass analysis (vector-like quarks)
(Skiba and Tucker-Smith PR D75 2007)
 - similar to chargino- neutralino production, when χ^0 is the LSP
 - like sign lepton final states, similar to 4th generation leptons
(Özcan, Aguilar-Saavedra, Aguila, Tuominen et al. ...)
- New decay channel(s) ($H \rightarrow \bar{\Psi}_S \Psi_D^0, \dots$) for the Higgs boson is possible